

Using Rates and Proportions

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This handout contains selected slides to use when reviewing this tutorial topic with or without the video. To access all slides, open thumbnail link on the tutorial interface.

Ratio

a comparison of two quantities

Ratios can be written in several ways.

using "to" 3 dogs to 2 cats

fraction form $\frac{3 \text{ dogs}}{2 \text{ cats}}$ or $\frac{3}{2}$

colon form 3 : 2

Each is read as "3 to 2"

Do not read the ratio $\frac{3}{2}$ as "three halves" as it is not a fraction.

Rate

a ratio comparing two different units

Example: exchange rate

\$4.63 US dollars is equal to £2.50 in British pounds

\$ 4.63 to £2.50

speed: 35 mph

35 miles per hour

35 miles traveled to 1 hour

air pressure: 34 psi

34 pounds per square inch

34 pounds to one square inch

Unit Rate

a rate in which the second term is one

mph and psi are examples of unit rates

Equivalent Ratios

$$\frac{34}{48} = \frac{17}{24} = \frac{51}{72}$$

Equivalent Ratios

$$\frac{\$ 12}{2 \text{ books}} = \frac{\$ 6}{\underset{\substack{| \\ \text{unit rate}}}{1 \text{ book}}}$$

Odds

the ratio of number of favorable outcomes (successes) to the number of unfavorable outcomes (failures)

Odds

Example: **30% chance of contracting a disease**

Odds of contracting the disease:

30 to 70

3 to 7

Slides from Using Rates and Proportions (Tutorial 17)

Using Ratios to Compare

There are 16 rabbits with white fur in a group of 34 rabbits.

16 rabbits with white fur out of a group of 34 rabbits

part-to-whole

16 white rabbits to 34 total rabbits

$$16 : 34 \quad \frac{16 \text{ white rabbits}}{34 \text{ total rabbits}}$$

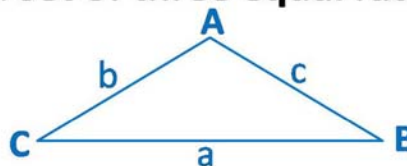
16 rabbits with white fur out of a group of 34 rabbits

part-to-part

16 white to 18 non-white

$$16 : 18 \quad \frac{16 \text{ white}}{18 \text{ non-white}}$$

The *Law of Sines* can be written as a set of three equal ratios.



$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

Proportion

two equal ratios

$$3 : 2 = 6 : 4$$

$$\frac{3}{2} = \frac{6}{4}$$

“3 is to 2 as 6 is to 4”

$$\frac{3}{2} = \frac{6}{4}$$

It is not proper to say three halves equals six fourths

These are not fractions!

Slides from Using Rates and Proportions (Tutorial 17)

Using Proportions to Solve Problems

Example: Exchange Rate

\$4.63 (US dollars) equals
£2.50 (British pounds)

*How many pounds are
exchanged for \$100?*

$$\frac{\$4.63}{£2.50} = \frac{\$100}{x} \quad \left. \vphantom{\frac{\$4.63}{£2.50}} \right\} \begin{array}{l} \text{two equal ratios} \\ \text{comparing} \\ \text{dollars to pounds} \end{array}$$

$$\frac{\$4.63}{£2.50} = \frac{\$100}{x} \quad \left. \vphantom{\frac{\$4.63}{£2.50}} \right\} \begin{array}{l} \text{two equal ratios} \\ \text{comparing} \\ \text{dollars to pounds} \end{array}$$

x = number of pounds
equal to \$100

$$\frac{\$4.63}{£2.50} \cdot £2.50x = \frac{\$100}{x} \cdot £2.50x$$

multiply both sides by £2.50x

$$\frac{\$4.63}{£2.50} \cdot \frac{£2.50x}{1} = \frac{\$100}{x} \cdot \frac{£2.50x}{1}$$

$$\frac{\$4.63}{1} \cdot \frac{£2.50x}{£2.50} = \frac{\$100}{1} \cdot \frac{£2.50x}{x}$$

Tutorials for High School Mathematics

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$$\frac{\$4.63}{\pounds 2.50} \cdot \frac{\pounds 2.50x}{1} = \frac{\$100}{x} \cdot \frac{\pounds 2.50x}{1}$$

$$\frac{\$4.63}{1} \cdot \frac{\cancel{\pounds 2.50}x}{\cancel{\pounds 2.50}} = \frac{\$100}{1} \cdot \frac{\pounds 2.50\cancel{x}}{\cancel{x}}$$

$$4.63x = 100 \cdot 2.50$$

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$$4.63x = 250$$

$$x = \frac{250}{4.63}$$

$$x \approx 53.995678$$

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$$4.63x = 250$$

$$x = \frac{250}{4.63}$$

$$x \approx 53.995678$$

$$x \approx 54 \text{ pounds}$$

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**\$100 US dollars can be
exchanged for approximately
£54.00 pounds**

**Five of every nine people
have type O⁺ blood.**

*In a population of 634,000
people, how many would
be expected to have type
O⁺ blood?*

$$\frac{5}{9} = \frac{t}{634,000}$$

t = people expected to have type O⁺

$$9t = 5 \cdot 634,000$$

$$t = 352222.\bar{2}$$

$$t \approx 352,222 \text{ people}$$

$$t \approx 352,222$$

**About 352,222 people
have type O⁺ blood**

Direct Variation

$$\frac{y}{x} = \frac{k}{1}$$

**Demonstrates a proportional
relationship between x and y
and a constant, k , the constant
of proportionality**

Direct Variation

$$\frac{y}{x} = \frac{k}{1} \rightarrow y = kx$$

**The graph of this equation is a
line with slope k passing through
the origin.**

Summary

- **How to use unit rates**
- **How to set up a ratio**
- **How to set up and solve a proportion**