

Self-Check for Tutorial 21

Logarithms

Note: Use the logarithm rules in the video tutorial to solve these problems. There are other rules for working with logarithms. After working through the problems in this Self-Check, consult a text book for additional rules or properties for working with both common and natural logarithms.

1. The population of a certain bacteria doubles every 10 minutes. How long will it take a population of 200 to reach 1,638,000? Use the formula $F = B \cdot (2)^T$ where F is the final count, B is the beginning count, and T is the number of times the bacteria must double.
 2. $A = P(e)^{rt}$ is the formula for continuous compounding interest. A is the final amount, P is the initial amount, r is the interest rate as a decimal and t is the time in years. If \$500 is put in the bank at a rate of 5% and the money is compounded continuously, how long will the money need to be in the bank to grow to \$2000?
3. Solve $5^{x+3} = 7^{3x-5}$ for x .

Answers to Self-Check for Tutorial 21

Logarithms

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1. The population of a certain bacteria doubles every 10 minutes. How long will it take a population of 200 to reach 1,638,000? Use the formula $F = B \cdot (2)^T$ where F is the final count, B is the beginning count, and T is the number of times the bacteria must double.

$$1,638,000 = 200 \cdot (2)^T$$

$$8192 = 2^T$$

$$\log_2(8192) = \log_2(2^T)$$

$$\log_2(8192) = T \log_2(2)$$

$$\log_2(8192) = T$$

$$\frac{\log_{10}(8192)}{\log_{10}(2)} = T$$

$$13 = T$$

If $T = 13$, the bacteria will double in 13 ten-minute periods or 2 hours and 10 minutes.

Note: By definition
 $\log_2(2) = 1$

Apply change-of-base rule

2. $A = P(e)^{rt}$ is the formula for continuous compounding interest. A is the final amount, P is the initial amount, r is the interest rate as a decimal and t is the time in years. If \$500 is put in the bank at a rate of 5% and the money is compounded continuously, how long will the money need to be in the bank to grow to \$2000?

$$2000 = 500(e)^{.05t} \text{ solve for } t$$

$$\frac{2000}{500} = e^{.05t}$$

$$4 = e^{.05t}$$

$$\ln(4) = \ln(e)^{.05t}$$

$$\ln(4) = .05t$$

$$\frac{\ln(4)}{.05} = t$$

$$27.72588722 = t$$

Therefore, \$500 will become \$2000 in approximately 27.73 years with continuous compounding.

Answers to Self-Check for Tutorial 21 Logarithms

3. Solve $5^{x+3} = 7^{3x-5}$ for x .

$$\log(5^{x+3}) = \log(7^{3x-5})$$

$$(x+3) \cdot \log(5) = (3x-5) \cdot \log(7)$$

$$x \log(5) + 3 \log(5) = 3x \log(7) - 5 \log(7)$$

$$x \log(5) - 3x \log(7) = -3 \log(5) - 5 \log(7)$$

$$x(\log(5) - 3 \log(7)) = -3 \log(5) - 5 \log(7)$$

$$x = \frac{-3 \log(5) - 5 \log(7)}{(\log(5) - 3 \log(7))}$$

$$x = 3.442965302$$